# MATRIX METHOD OF LASER FLUORIMETRY OF COMPLEX ORGANIC COMPOUNDS IN WATER

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#### ABSTRACT

A matrix method synthesizing methods of kinetic and non-linear laser fluorimetry is presented in this paper. It is assumed that in the case of a rational selection of the range for photon flux density of the exciting radiation, and of the range of time for measurements of fluorescence kinetics, it is possible to determine a substantial number of molecular photo-physical parameters of complex organic compounds. This could be achieved by solving the inverse problems with the elements of the suggested matrix as input data. As a first step in the development of this approach, numerical modelling of the direct and inverse problems has been performed using the model of a two-fluorophore complex with intermolecular energy transfer.

**Keywords:** matrix method of fluorescence, fluorescence of organic compounds, photo-physical parameters

#### INTRODUCTION

This work was stimulated by the necessity to increase the information content of fluorimetry for the analysis of natural organic compounds (NOC) – dissolved organic matter (DOM), oil complexes (films, emulsions), protein compounds etc. The traditional spectral analysis has limited opportunities here. For example, different types of DOM (allochtonous/autochtonous, labile/stable etc.) have close fluorescence bands.

In our previous studies (1,2,3), we suggested to use molecular photo-physical parameters – absorption cross sections, lifetimes of excited states etc. for NOC diagnostics, which can be determined by solving the inverse problems of non-linear fluorimetry (1,2) or of kinetic fluorimetry (2,3). These parameters are important not only for NOC diagnostics, but also to study photo-physical processes in these compounds. In the last few years, we have used the technique of artificial neural networks (ANN, (4)) to solve such problems (1,2,3).

It is well known that any method of solution of inverse problems requires *a priori* information about the object of study. The amount of such information available from most types of NOC is very small. In many cases such as DOM, oil complexes etc. there is no reliable information about the number of fluorophores, their fluorescence spectra and the orders of magnitude of the main photophysical parameters.

The kinetic curves and the fluorescence saturation curves of NOC are of such nature that even when the ANN algorithms are used it is only possible to determine two or three photo-physical parameters with satisfactory precision.

### THE MATRIX MODEL

In principle, we describe the fluorescent response of NOC with a model including several fluorophores. Connecting this model to real fluorophores is a different and very complicated task. At present we consider it optimal to use the two-fluorophore model for a number of reasons. Mathematically it is described by a system of kinetic equations:

$$\begin{cases} \frac{dn_1}{dt} = F(t)\sigma_1(n_{01} - n_1) - \frac{n_1}{\tau_1} - \gamma_1 n_1^2 - K_{12}n_1(n_{02} - n_2) \\ \frac{dn_2}{dt} = F(t)\sigma_2(n_{02} - n_2) - \frac{n_2}{\tau_2} - \gamma_2 n_2^2 + K_{12}n_1(n_{02} - n_2) \end{cases}$$

with:  $n_1, n_2$  concentrations of the excited molecules of the corresponding fluorophores;  $n_{01}, n_{02}$  initial concentrations of the molecules of the corresponding fluorophores;

 $\tau_1$ ,  $\tau_2$  lifetimes of the excited molecules of the corresponding fluorophores;

- $\gamma_1, \gamma_2$  constants of singlet-singlet annihilation of the corresponding fluorophores;
- $\sigma_1$ ,  $\sigma_2$  excitation cross sections of the corresponding fluorophores;
- F(t) photon flux density of the exciting radiation;
- $K_{12}$  constant of intermolecular energy transfer from the first to the second fluorophore.

Having determined  $n_1(t,F)$  and  $n_2(t,F)$ , it is possible to calculate the fluorescence intensity I(F,T) in a receiver gate delayed for time T with respect to the exciting laser pulse for the given value of photon flux density F (refer to (3)).

In this model we do not separate intercombinative (S-T) conversion from common channel of intermolecular relaxation of excited state of fluorophores, i.e. from common time of this relaxation  $\tau_1$ and  $\tau_2$ . Nevertheless, there are nine model parameters, which cannot be determined simultaneously neither with the kinetic fluorimetry method, nor with the nonlinear fluorimetry method, nor by the sequential use of these methods. These considerations have led us to the idea to perform a synthesis of these methods. To do so, the following matrix needs to be measured:

$$\mathbf{M}_{FT} = \begin{bmatrix} I_{F_1T_1} & \cdots & I_{F_1T_t} \\ \vdots & \vdots & \vdots \\ I_{F_wT_1} & \cdots & F_{F_wT_t} \end{bmatrix}$$

where  $I_{F_nT_m}$  is the fluorescence intensity of the organic compounds mixture for the exciting radiation photon flow density  $F_n$  and for the strobe delayed for time  $T_m$  with respect to the laser pulse.

The rows of this matrix are the points on kinetic curves at different photon flux densities F; the columns are the points on fluorescence saturation curves at different strobe delays T. The range of Fshould be selected in such a way that at its minimal value there would be no saturation of fluorescence, and at its maximal value saturation would be significant. The degree of saturation at maximal F is chosen based on the peculiarities of the specific problem.

From physical considerations it may be expected that different matrix elements have different dependences on photo-physical parameters. Consequently, under rational choice of matrix elements, all photo-physical parameters can be determined. In this paper, the first steps in the development of this approach have been made.

It should be noted that this approach is in principle different from the matrix method (5,6), where the following matrix is used:

$$\mathbf{M}_{\lambda T} = \begin{bmatrix} I_{\lambda_1 T_1} & \cdots & I_{\lambda_1 T_t} \\ \vdots & \vdots & \vdots \\ I_{\lambda_w T_1} & \cdots & F_{\lambda_w T_t} \end{bmatrix}$$

#### RESULTS

By numerical modelling, the following blocks (sections) of the full problem of elaboration of the suggested matrix method have been considered.

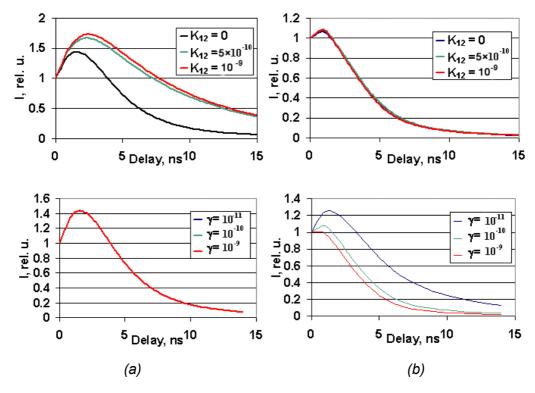


Fig.1 Kinetic curves of the fluorescence of organic compounds, calculated at  $F=10^{21} \text{ cm}^{-2}\text{s}^{-1}$  (a) and  $F=10^{25} \text{ cm}^{-2}\text{s}^{-1}$  (b) with different values of intramolecular parameters.

Consideration of the direct problem illustrates the fact that different matrix elements have different dependences on the chosen photo-physical parameters. Such consideration was carried out for the constants of intermolecular interactions, which have never been determined in kinetic and nonlinear fluorimetry before. The corresponding parameters are:  $K_{12}$  and  $\gamma_1 n_{01}$ ,  $\gamma_2 n_{02}$ . Figure 1 displays the kinetic curves calculated at different values of F:  $10^{21}$  cm<sup>-2</sup>s<sup>-1</sup>, where fluorescence saturation is absent, and  $10^{25}$  cm<sup>-2</sup>s<sup>-1</sup> where saturation manifests itself significantly. As shown in the figures, at small values of F the constant  $K_{12}$  of intermolecular transfer of energy from the first fluorophore to the second one significantly influences the kinetic curves. At the same time, these kinetic curves do not depend on the singlet-singlet annihilation constants at all. At large values of F, the kinetic curves depend on all the three mentioned parameters, but differently.

Table 1 contains typical values of photo-physical parameters for several organic compounds (dyes and natural compounds) as reported in literature.

Table 1.	Typical values	of photo-physical	parameters for s	some organic compo	unds
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	τ, ns	$\sigma$ , cm <sup>2</sup>	<i>K</i> <sub>12</sub> , s <sup>-1</sup>
Rhodamine 6G (in water) (7)	5.4	0.5·10 <sup>-16</sup> (at λ=530 nm)	10 <sup>7</sup>
Eosine (8)	2.58	-	7.61·10 <sup>8</sup>
Stilbene 3 (9)	12.5	(2.3±0.3) ·10 <sup>-16</sup>	-
Amino G acid (9)	1.1	1.10 10 <sup>-17</sup>	-
Tryptophane (in water) (10)	2.6	-	-
Phytoplankton	0.25	-	-
Humic substance (11)	τ <sub>1</sub> =2.8; τ <sub>2</sub> =4.4	$\sigma_1 = 3.7 \cdot 10^{-17}; \sigma_2 = 2.9 \cdot 10^{-17}$	-
5H-Dibenzo[a,d]cyclohepten-5-one (12)	17 ± 6	-	-
Angular dimers of dyes (13)	15	-	10 <sup>9</sup> 10 <sup>11</sup>

Our first approbation of the opportunities of the matrix method in the solution of this inverse problem has been performed for 5 parameters: the lifetimes of both fluorophores  $\tau_1$  and  $\tau_2$ , the constants of singlet-singlet annihilation  $\gamma_1$  and  $\gamma_2$ , and the constant of intermolecular energy transfer from the first fluorophore to the second one  $K_{12}$ . The remaining four of the above specified nine intermolecular parameters of the mixture of organic compounds were considered to be known, their values are given in Table 2 (upper left corner). The ranges of the target parameters are also presented in Table 2, their determination has been addressed in (3).

For numerical modelling, the following parameters of laser radiation and of the receiver were used: laser pulse duration  $t_p=10$  ns; its shape was considered to be Gaussian; gate integration time  $t_g=10$  ns; gate positioning step 2 ns. The matrix elements that were used corresponded to five kinetic curves without noise and with 5% noise, obtained at five photon flux densities of laser radiation.

To solve the five-parameter inverse problem, genetic algorithms (GA, (14)) were used. The advantage of GA in comparison to other methods of solving inverse problems, in particular, in comparison to ANN, is its high efficiency for solution of multi-parameter problems (the ANN technique is successfully used for determination of two or three parameters). The results of solving the fiveparameter inverse problem are presented in Table 2.

Fixed parameters: $\sigma_1 = 10^{-16} \text{ cm}^2$ , $\sigma_2 = 10^{-17} \text{ cm}^2$ , $n_{01} = n_{02} = 10^{18} \text{ cm}^{-3}$	Errors of determination of the target parameters at different noise level in input data		
target parameters and their ranges	Noise level 0%	Noise level 5%	
$\tau_1$ (10 <sup>-11</sup> 10 <sup>-7</sup> ) s	2%	25%	
$ au_2$ (10 <sup>-11</sup> 10 <sup>-7</sup> ) s	0%	25%	
$\gamma_1$ (10 <sup>-11</sup> 10 <sup>-8</sup> ) cm <sup>3</sup> /s	10%	30%	
$\gamma_2$ (10 <sup>-11</sup> 10 <sup>-8</sup> ) cm <sup>3</sup> /s	10%	20%	
$K_{12}$ (10 <sup>-11</sup> 10 <sup>-8</sup> )	20%	60%	

Table 2: The results of solving the five-parameter inverse problem.

Thus, we succeeded in simultaneous determination of 5 parameters with acceptable precision using 75 elements of the matrix (5 kinetic curves, 15 points each).

It should be noted that the higher the number of elements in the matrix, the higher is the precision of determination of the parameters. An increase in the number of the delays primarily causes an increase in the precision of determination of lifetimes; the number of photon fluxes primarily influences the precision of measurement of other parameters. In fact, the dimensions of the matrix should be determined based on the acceptable error levels for all the determined parameters. However, we do not have any formula yet to make an estimation of the required matrix dimensions; the required size of the matrix has been determined by a numeric experiment.

The ANN method gives better precision, but for fewer parameters. Therefore, we suppose to consider the opportunity of implementing the procedure of step-by-step determination of the parameters by groups of three parameters, using "blocks" of matrix elements chosen on the base of physical considerations.

# CONCLUSIONS

The first steps made in the direction of creating a matrix method, synthesizing laser kinetic and non-linear fluorimetry, demonstrate the perspective of this approach. The experience accumulated while performing this work, has shown that the development of the suggested matrix method would be quite difficult. However, the efforts are justified by the possibility to determine a large number of photo-physical parameters, which can be used to characterize natural organic compounds. At present, no alternative is seen to this approach.

## ACKNOWLEDGEMENTS

This work was performed with support from the Russian Foundation of Basic Research (projects No. 02-05-64430a, 03-02-16628a).

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